Efficient Meta Learning via Minibatch Proximal Update

Pan Zhou

Joint work with Xiao-Tong Yuan, Huan Xu, Shuicheng Yan, Jiashi Feng

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update task-specific solution

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• **Benefit:** a few data is sufficient for adaptation

prior model $oldsymbol{w}\,$ is close to optimum $oldsymbol{w}_T$

when training and test tasks are from a same distribution \mathcal{T} .



We use SGD based algorithm to solve bi-level training model :

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- Step2. for T_i , compute an approximate minimizer: $\boldsymbol{w}_{T_i} \approx \operatorname{argmin}_{\boldsymbol{w}_{T_i}} \{g(\boldsymbol{w}_{T_i}) =: \mathcal{L}_{D_{T_i}}(\boldsymbol{w}_{T_i}) + \frac{\lambda}{2} \|\boldsymbol{w} - \boldsymbol{w}_{T_i}\|_2^2 \} \text{ s.t. } \|\nabla g(\boldsymbol{w}_{T_i})\|_2^2 \leq \epsilon_s$

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$$\boldsymbol{w} = \boldsymbol{w} - \eta_s \lambda (\boldsymbol{w} - \frac{1}{b_s} \sum_{i=1}^{b_s} \boldsymbol{w}_{T_i})$$

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Theorem 1 (convergence guarantees, informal).

(1) Convex setting, i.e. convex $\phi_{D_{T_i}}(\boldsymbol{w})$. We prove $\mathbb{E}[\|\boldsymbol{w}^S - \boldsymbol{w}^*\|_2^2] \leq \mathcal{O}(\frac{1}{S})$.

(2) Nonconvex setting, i.e. smooth $\phi_{D_{T_i}}(\boldsymbol{w})$. We prove $\mathbb{E}_s[\|\nabla F(\boldsymbol{w}^s)\|_2^2] \leq \mathcal{O}(\frac{1}{\sqrt{S}})$.

Generalization Performance Guarantee

- Ideally, for a given task T, one should train the model on the population risk Population solution: $\boldsymbol{w}_P^* = \operatorname{argmin}_{\boldsymbol{w}_T} \mathbb{E}_{(\boldsymbol{x}, \boldsymbol{y}) \sim T} \ell(f(\boldsymbol{w}_T, \boldsymbol{x}), \boldsymbol{y}).$
- In practice, we only has K samples and adapt the prior model w^* to the new task: Empirical solution: $w_T^* = \operatorname{argmin}_{w_T} \mathcal{L}_{D_T}(w_T) + \frac{\lambda}{2} \|w^* - w_T\|_2^2$.

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- Since $m{w}_P^*
 eq m{w}_T^*$, why $m{w}_T^*$ is good for generalization in few-shot learning problem?

Theorem 2 (generalization performance guarantee, informal). Suppose each loss $\phi_{D_{T_i}}(\boldsymbol{w})$ is convex and is smooth. Let $D_T = \{(\boldsymbol{x}_i, \boldsymbol{y}_i)\}_{i=1}^K \sim T$. Then we have $\mathbb{E}_{T \sim \mathcal{T}} \mathbb{E}_{D_T \sim T} (\mathcal{L}(\boldsymbol{w}_T^*) - \mathcal{L}(\boldsymbol{w}_P^*)) \leq \frac{c}{\sqrt{K}} \mathbb{E}[\|\boldsymbol{w}^* - \boldsymbol{w}_P^*\|_2^2].$

Remark: strong generalization performance, as our training model guarantee

prior $oldsymbol{w}^*$ is close to the optimum model $oldsymbol{w}_P^*$.

Experimental results

Few-shot regression : smaller mean square error (MSE) between prediction and ground truth



Few-shot classification: higher classification accuracy





POSTER # 26

05:00 -- 07:00 PM @ East Exhibition Hall B + C

Thanks!